

Thinning or thickening? Complex rheology of dense suspensions

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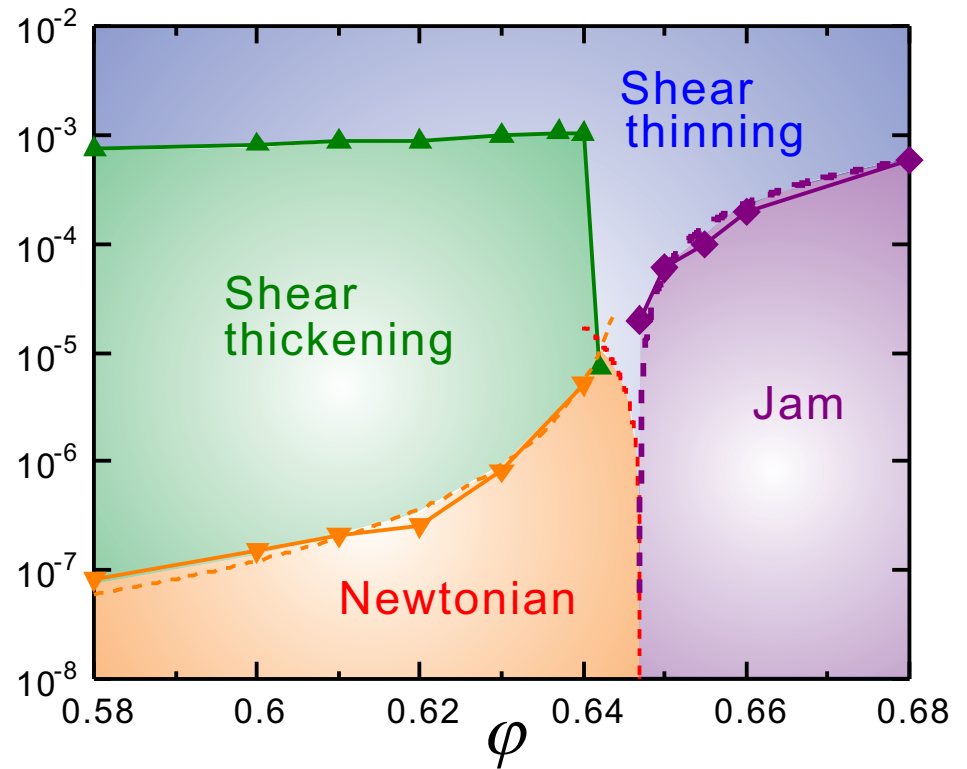
Coworkers

• With:

T. Kawasaki (Montpellier)

A. Ikeda (Montpellier)

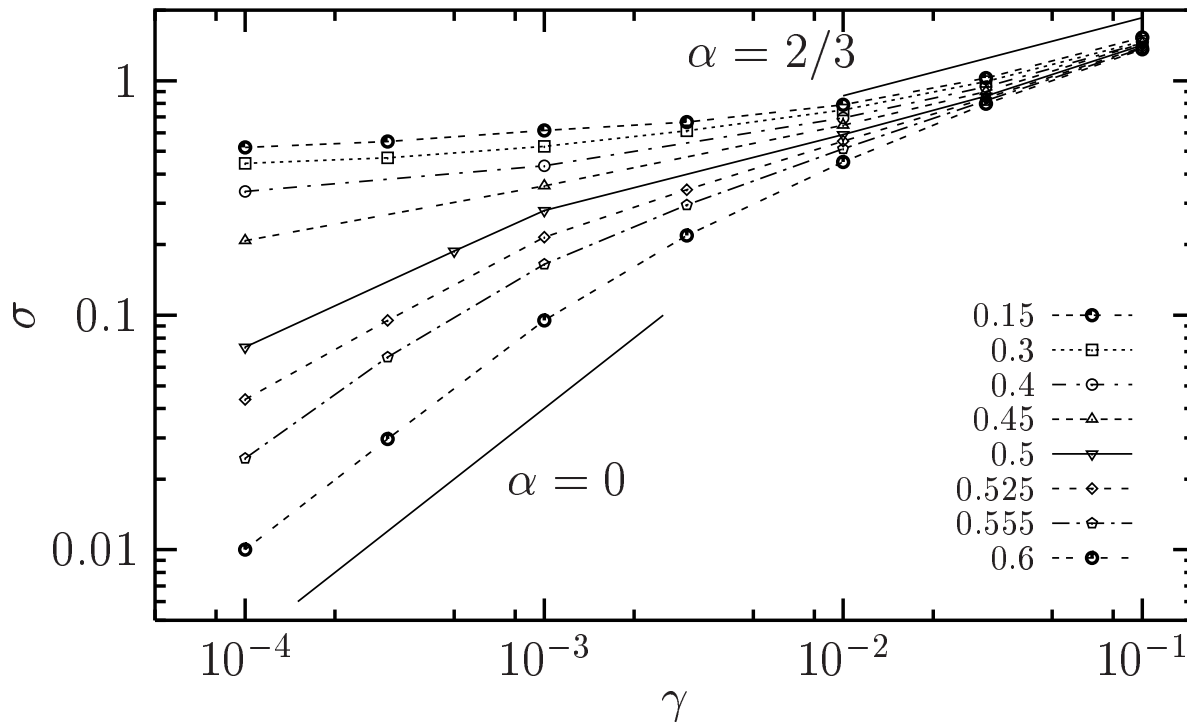
P. Sollich (London)



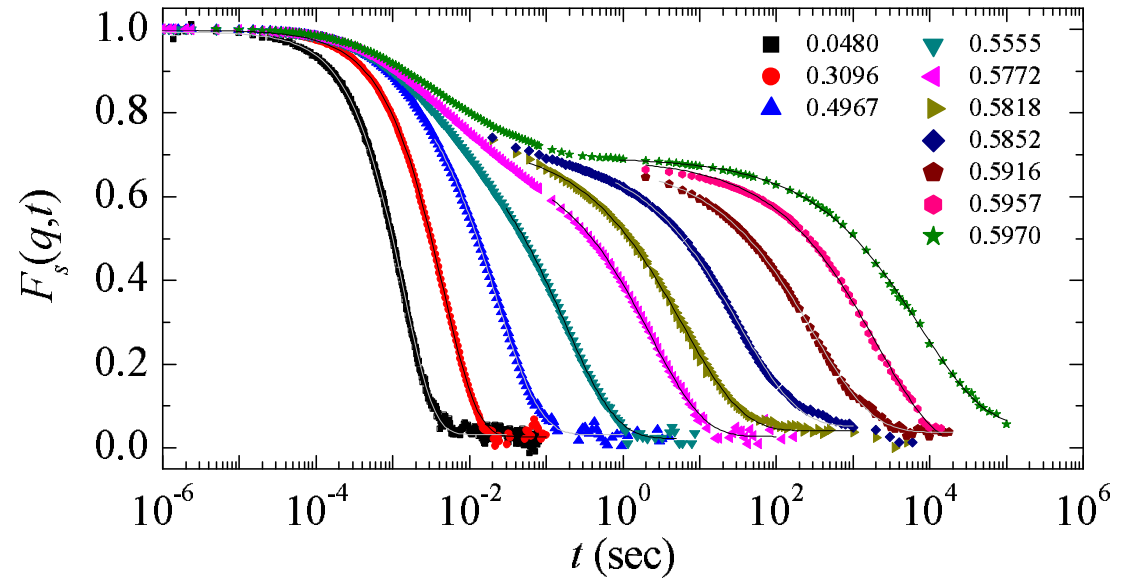
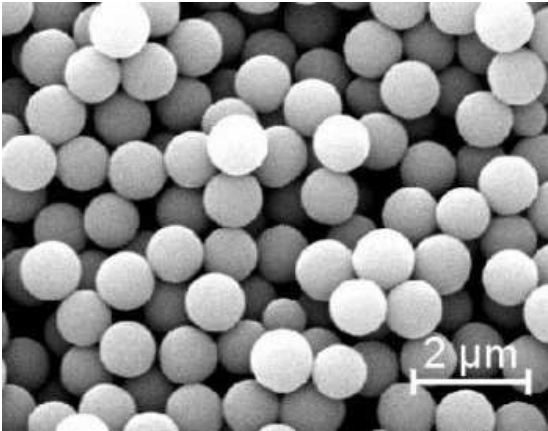
[Kawasaki, Ikeda, Berthier, arXiv:1404.4778]

Nonlinear glassy rheology

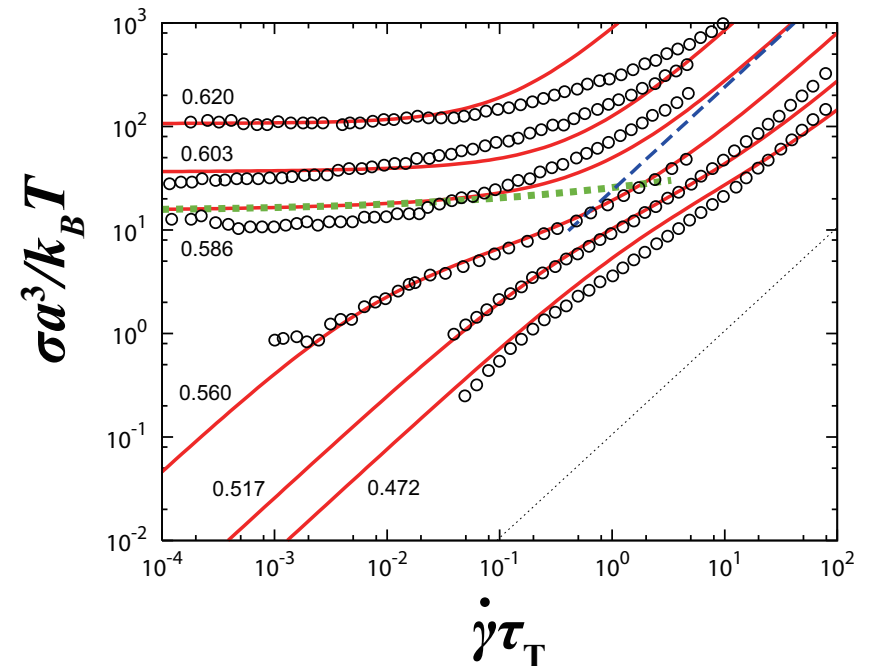
- Decreasing T in **supercooled liquids**: ‘Diverging’ viscosity $\eta(T)$.
- Transition from **viscous** fluid to **solid** material (finite yield stress).
- **Flow curves** at finite shear rate $\dot{\gamma}$ in simple shear flow: $\sigma = \sigma(\dot{\gamma}) = \eta(\dot{\gamma})\dot{\gamma}$, in binary LJ mixture. Viscosity is a function.



Dense colloidal suspensions



- Colloidal (Brownian) glass transition upon compression.
- ‘Diverging’ viscosity: $\eta_T(\varphi)$.
- **Rheology** similar to molecular glasses: $\eta = \eta(\dot{\gamma}, \varphi)$.

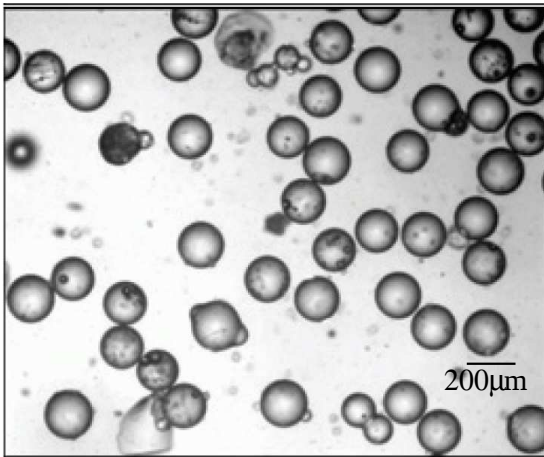


[Brambilla *et al.*, PRL '09]

[Petekidis *et al.*, JPCM '04]

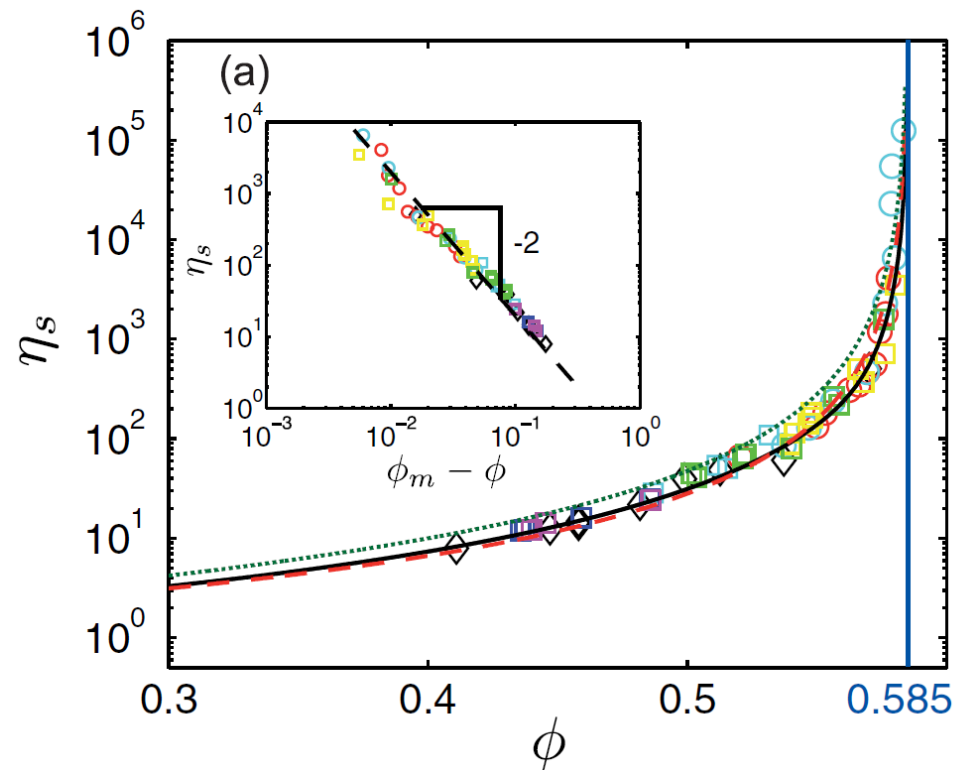
Granular suspensions

- Jamming transition: compressing **macroscopic** (non-Brownian) particles.
- Example: granular suspensions. ‘Diverging’ viscosity: $\eta_0(\varphi) \neq \eta_T(\varphi)$.



[Brown & Jaeger, PRL '09]

- Rigid particles: **linear** rheology $\eta = \eta_0(\varphi)$.

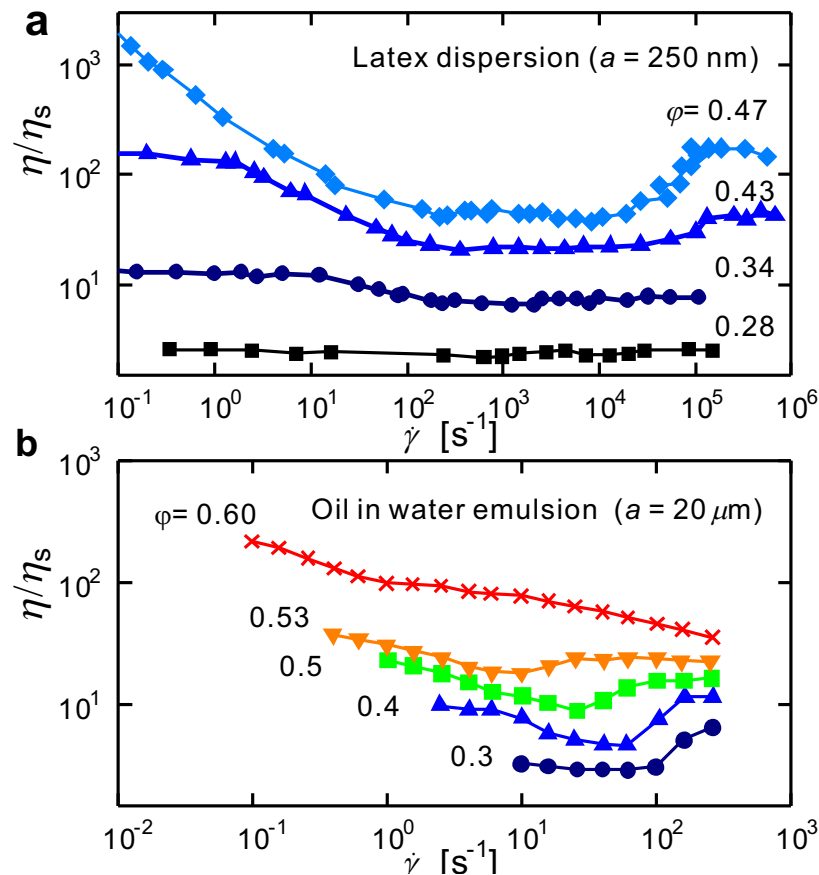


[Boyer & Pouliquen, PRL '10]

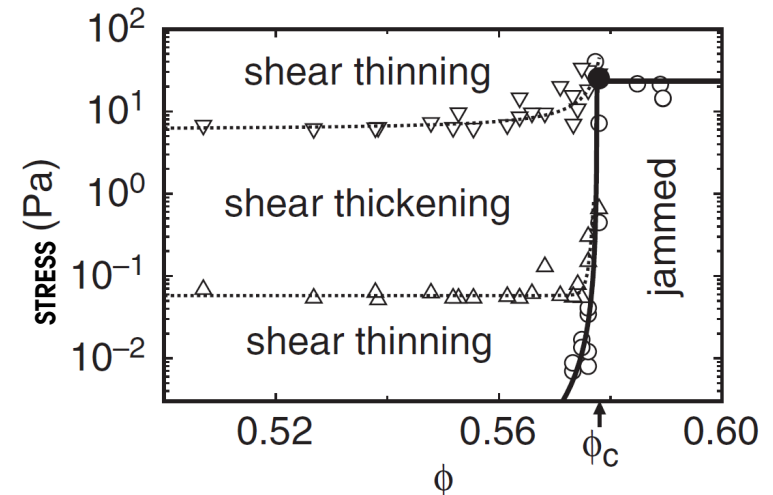
- Soft particles: Jamming transition from **viscous** to **solid** suspension (yield stress) with non-linear rheology: $\eta = \eta(\dot{\gamma}, \varphi)$, at $T = 0$.

Shear-thickening

- Observed in large variety of systems: soft/hard, large/small... Multiple 'complex' explanations: hydrodynamics, micro-structure...



[Wagner, Brady, Phys. Today '09]
[Otsubo, Rheol. Acta '94]



[Brown, Jaeger PRL '09]

- Thickening coexists with other regimes.
- Strong interplay with jamming.
- Role of friction for macroscopic particles: discontinuous thickening.

Simple numerical model

- To understand complex systems, one must understand simple ones...
- Langevin dynamics for **soft** harmonic spheres with **shear** and **temperature** in $d = 3$:

$$m \frac{d\mathbf{v}_i}{dt} + \xi(\mathbf{v}_i - \dot{\gamma} y_i \mathbf{e}_x) + \sum_j \frac{dV(|\mathbf{r}_i - \mathbf{r}_j|)}{d\mathbf{r}_i} + \eta_i = 0,$$

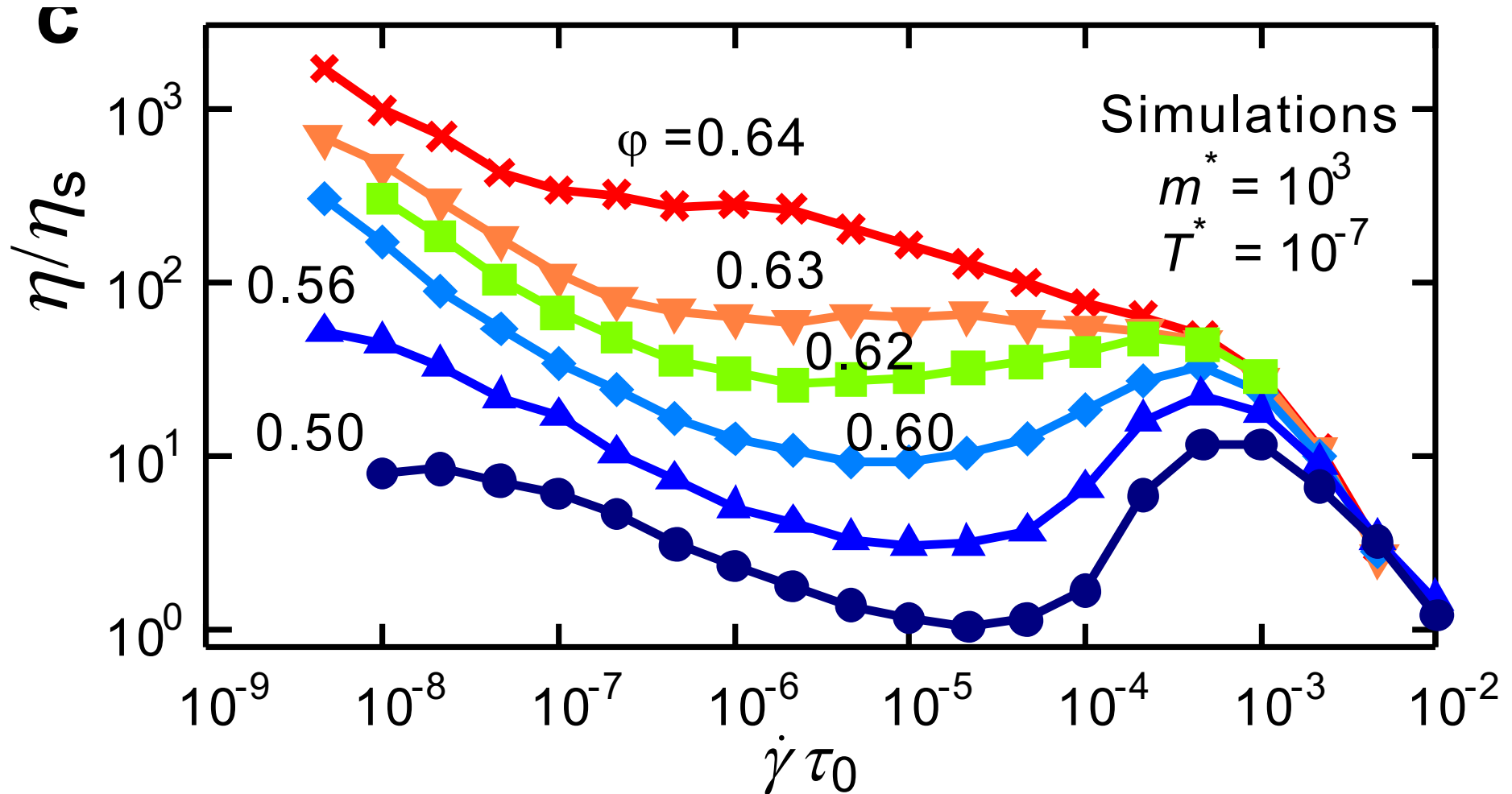
with $\langle \eta_i(t) \eta_j(t') \rangle = 2k_B T \xi \mathbf{1} \delta(t - t')$ and $V(r \leq a) = \epsilon(1 - r/a)^2$.

- Four microscopic **timescales**:

- (i) **dissipation**: $\tau_0 = \xi a^2 / \epsilon = 1$, our time unit.
- (ii) **thermal time**: $\tau_D = \xi a^2 / (k_B T) \rightarrow \infty$ when $T \rightarrow 0$.
- (iii) **velocity damping**: $\tau_v = m / \xi$.
- (iv) **shear rate**: $\dot{\gamma}$, competes with (i)-(iii).

- We can study both finite and zero temperature, both overdamped and inertial regimes within single model. Vary $\dot{\gamma}$ at constant (T, m) .

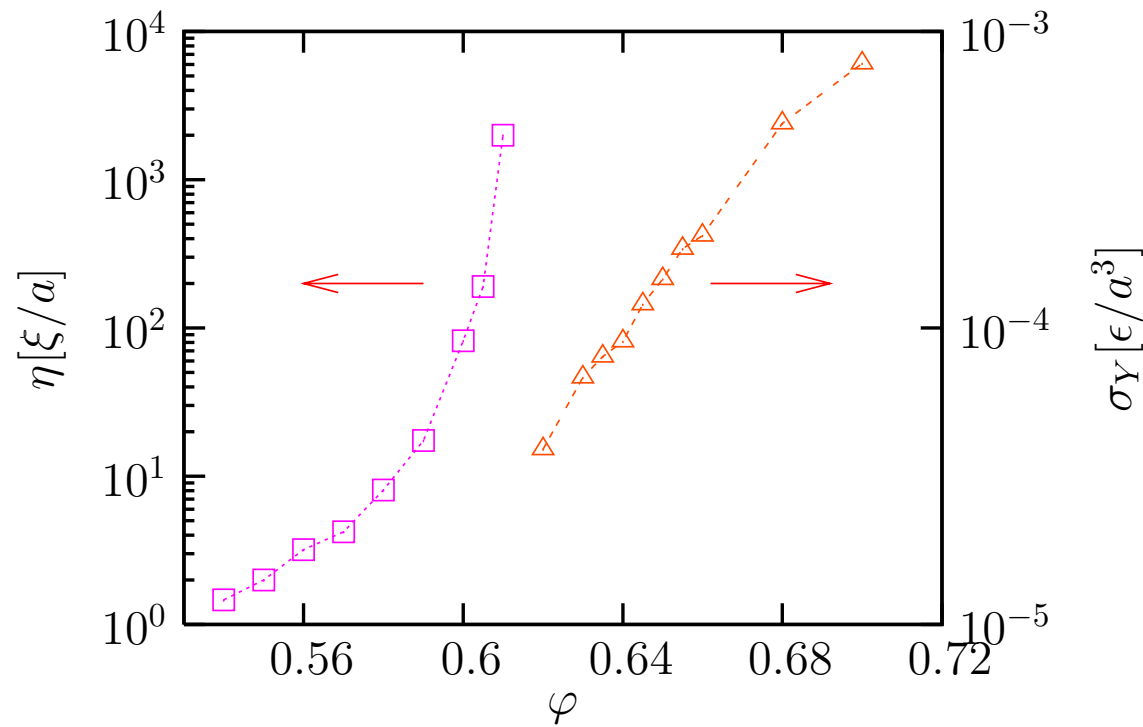
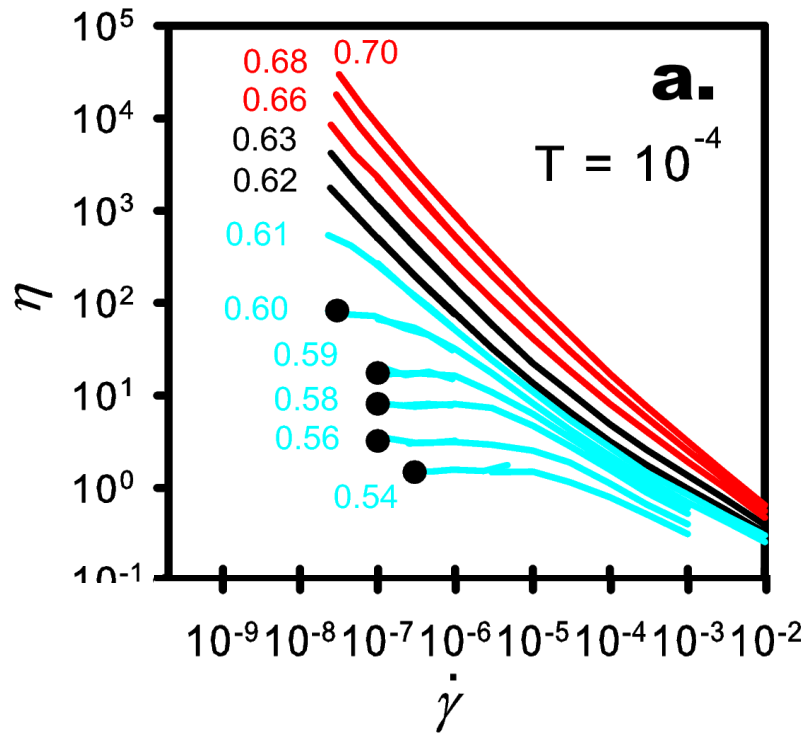
Multiple rheological regimes



- **Complex patterns** of Newtonian, shear-thinning, and shear-thickening regimes, with nontrivial density dependence.
- Qualitatively similar to experimental data.

Soft glassy rheology

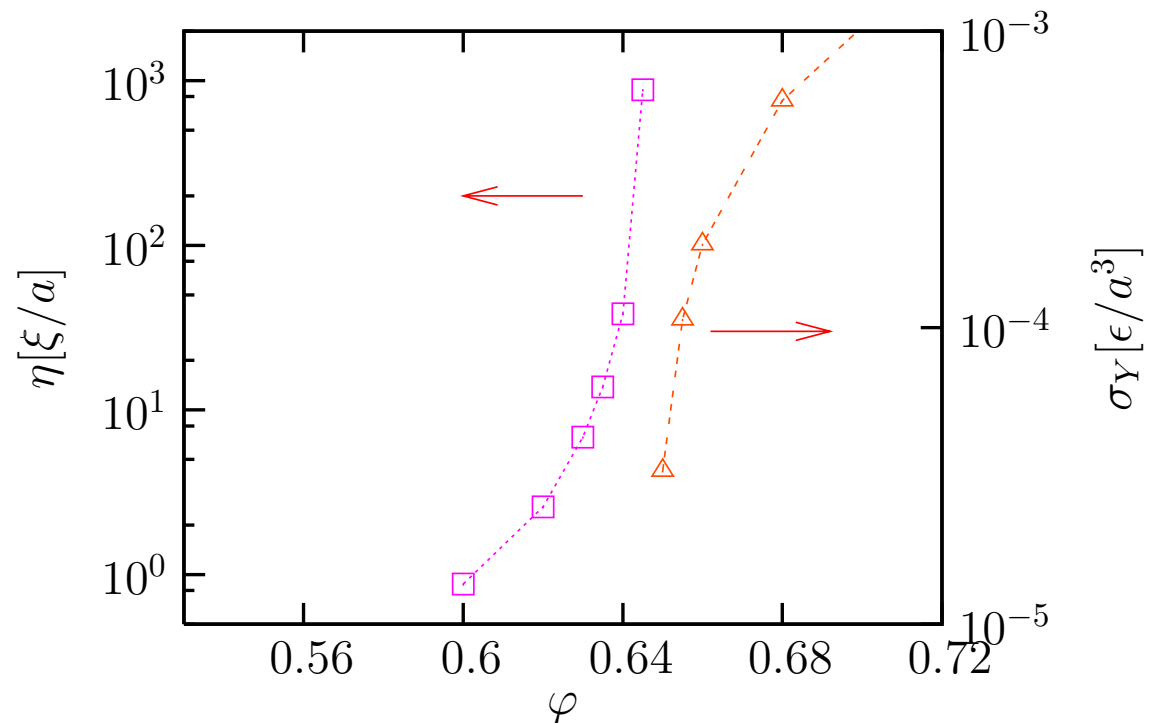
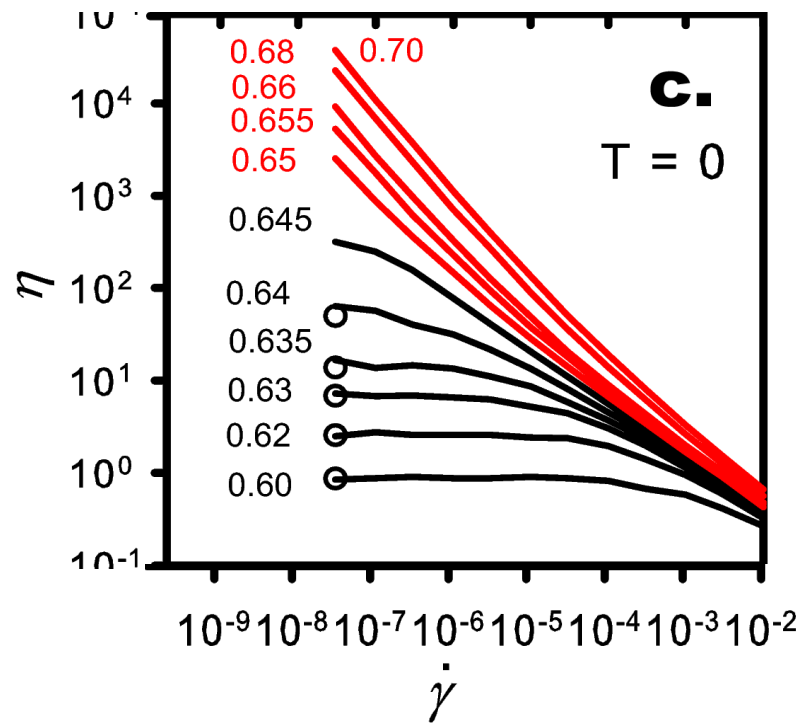
- Steady state rheology at $(T = 10^{-4}, m = 0)$. Diverging Newtonian viscosity and emerging yield stress as φ increases.



- Glassy rheology**, as seen in colloidal particles, star polymers, microgels, simple supercooled liquids: $\dot{\gamma}\tau_D \ll 1$.
- Theories of **driven glasses** capture competition between slow glassy dynamics and shear flow (reasonably) well.

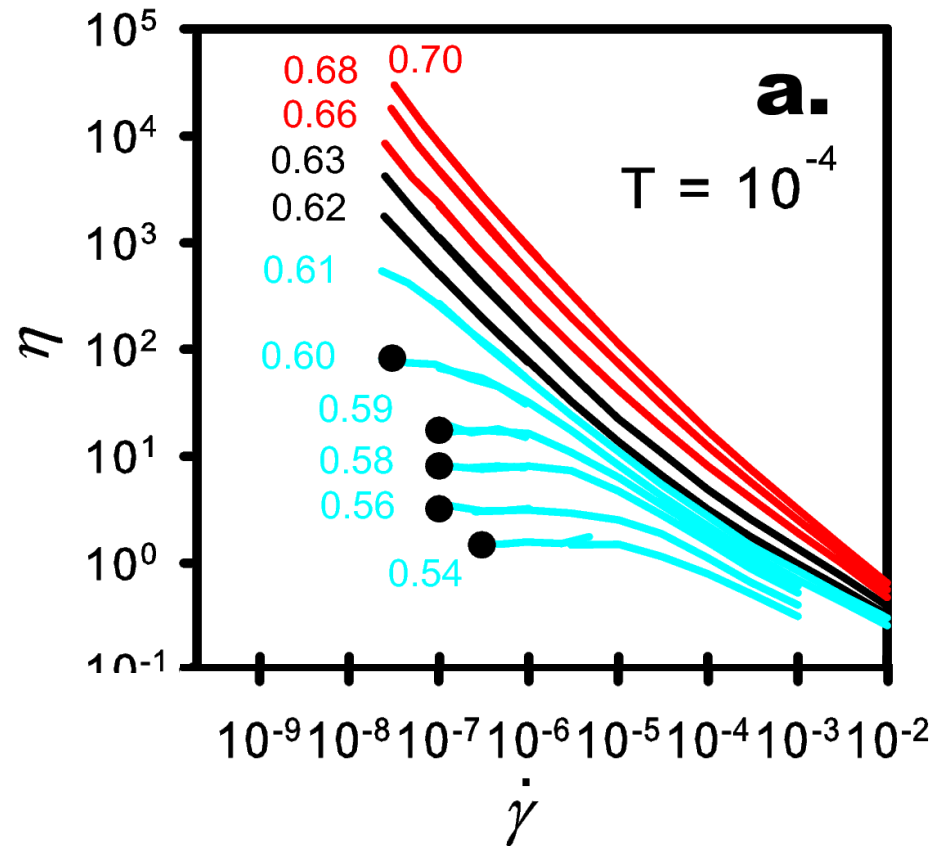
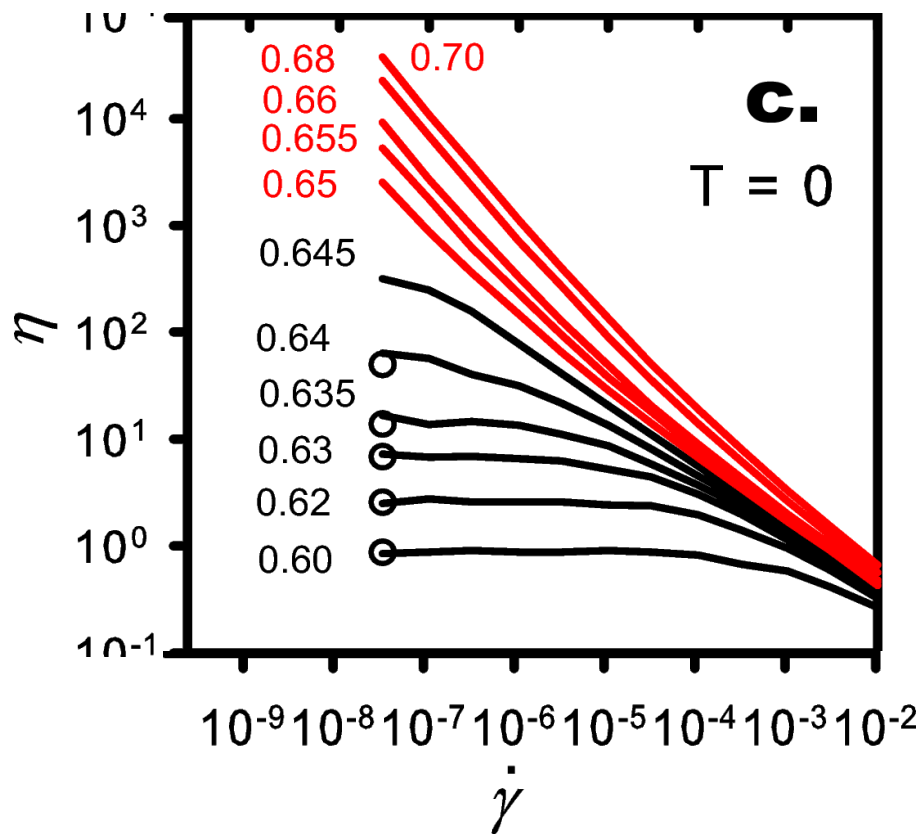
Non-Brownian suspension rheology

- Rheology at $(T = 0, m = 0)$. Diverging Newtonian viscosity and emerging yield stress as φ increases.



- Rheological signature of $T = 0$ jamming transition: $\dot{\gamma}\tau_D \gg 1$.
- **No microscopic theory** for rheology. Driven dynamics at $T = 0$ is difficult to attack from first principles, subtle structural changes under shear.

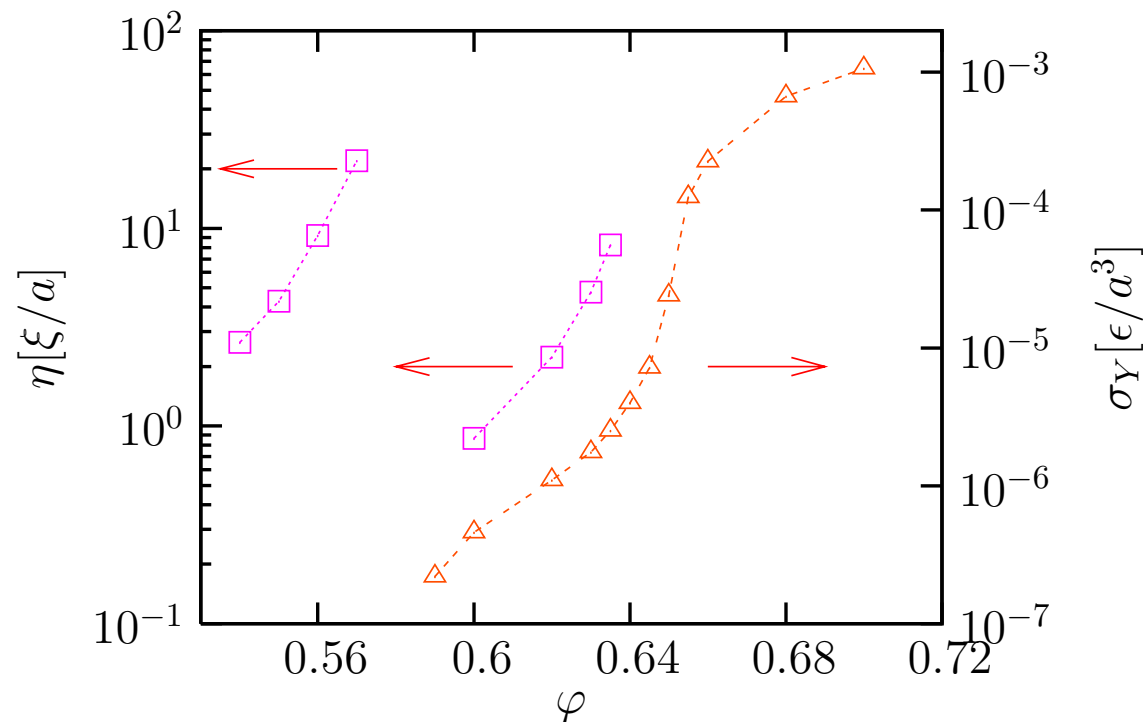
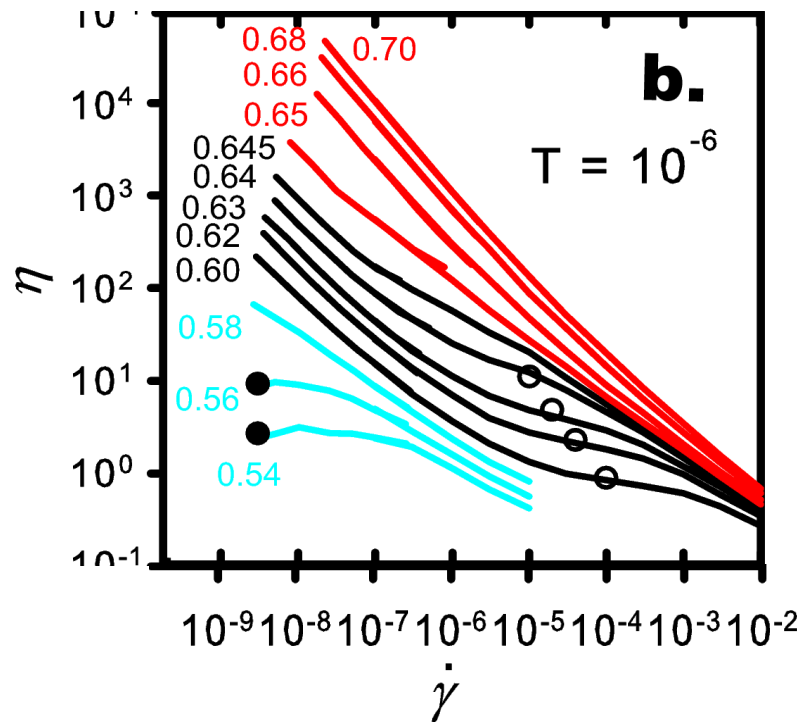
How confusing...



- It is crucial to understand stress & time scales, rather than the shape of the flow curves, in particular $\dot{\gamma} \tau_D \gg 1$ or $\dot{\gamma} \tau_D \ll 1$ makes a dramatic difference (from jamming to glass transitions).

Glass – jamming crossover

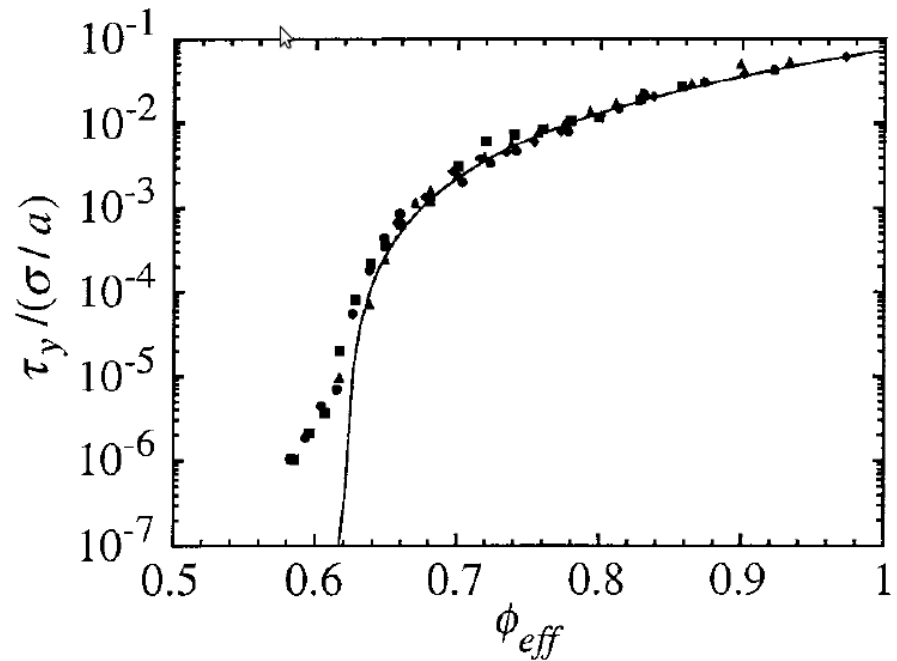
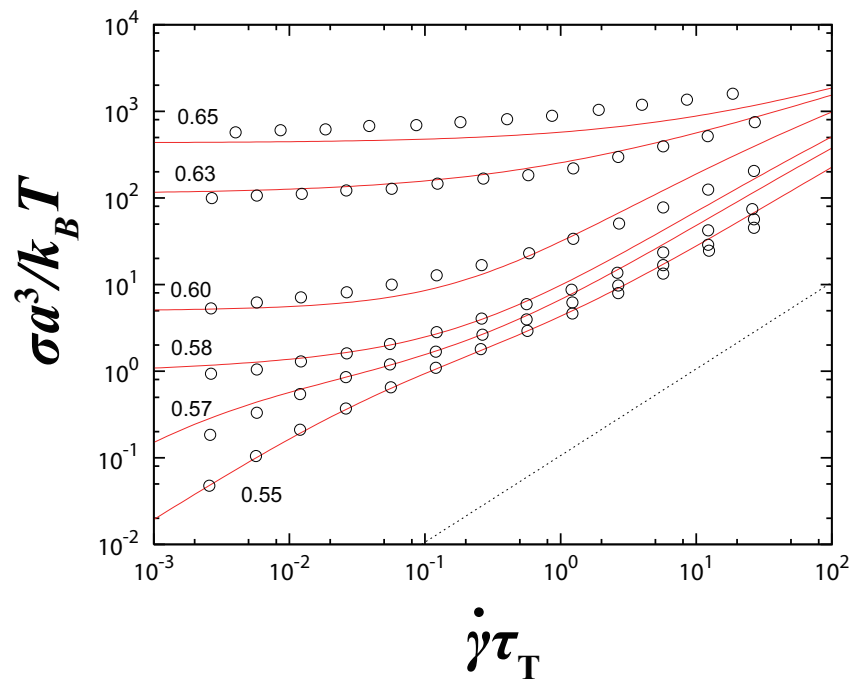
- Simulations at $(T = 10^{-6}, m = 0)$. Crossover from glassy physics when $\dot{\gamma}\tau_D \ll 1$ to athermal jamming physics when $\dot{\gamma}\tau_D \gg 1$.



- Two Newtonian regimes, **two distinct viscosities**, emergence of yield stress (when $\dot{\gamma} \rightarrow 0$), with strange density dependence. **Complex rheology...** even without inertia.

Crossover in experiments

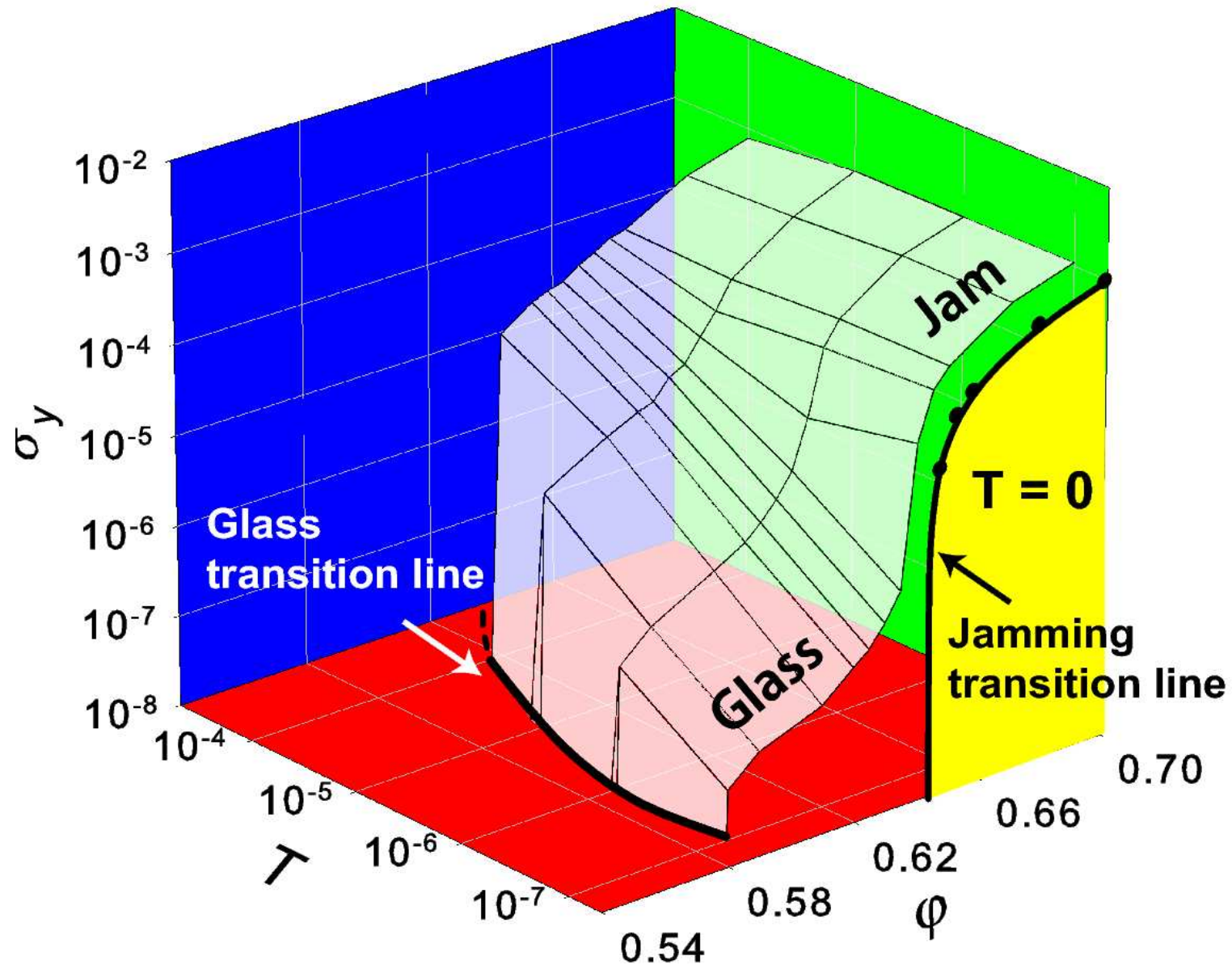
- **Microemulsions** ideal to observe the crossover: right size, right softness. Both **glass** and **jamming contributions needed** to describe rheology.



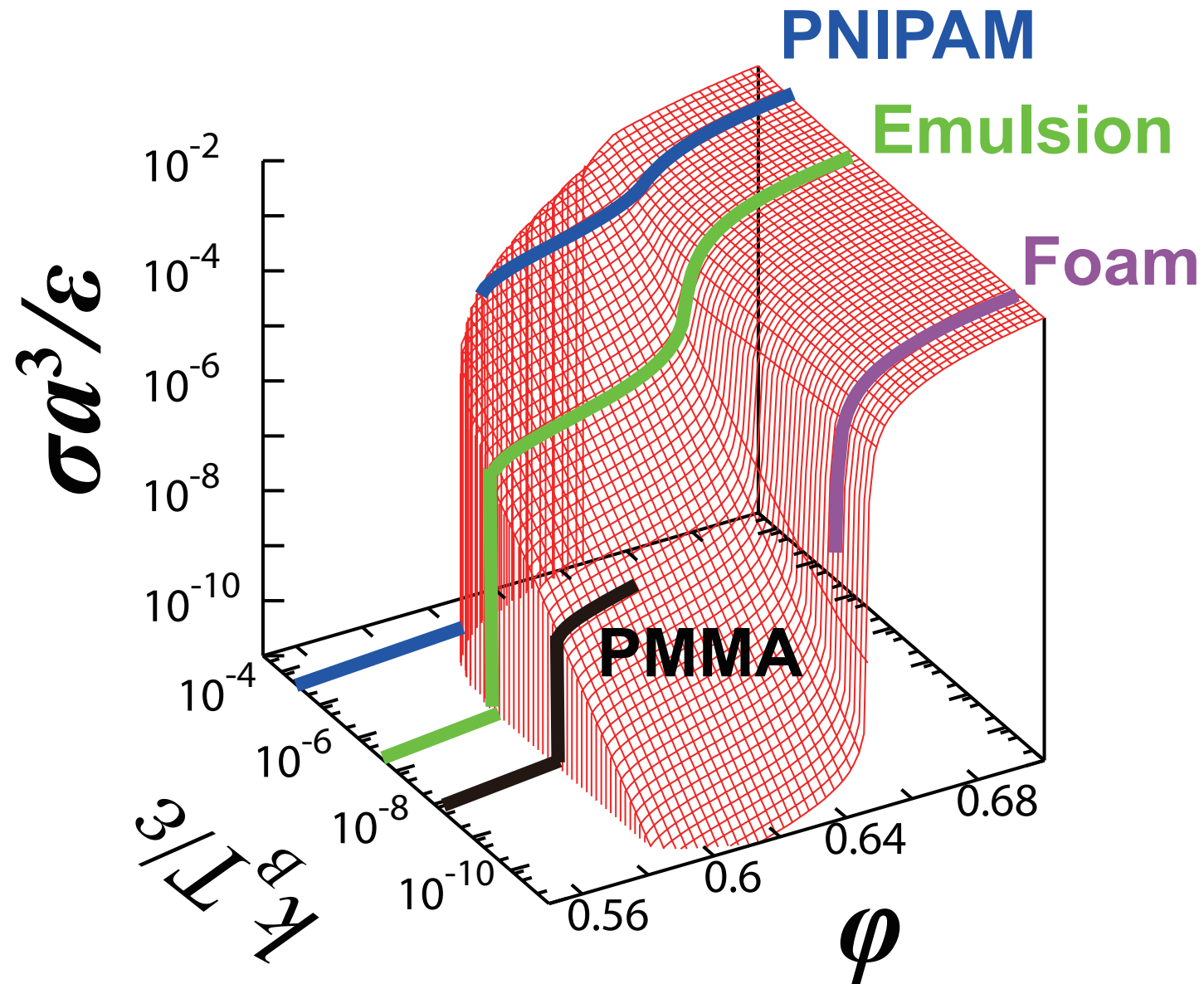
[from Mason, Bibette, Weitz, 1996]

- **Star polymers** and **pnipam microgels** are too soft, **grains/foams** are too large. Either glass or jamming, but one must choose the right one...

'Jamming phase diagram'

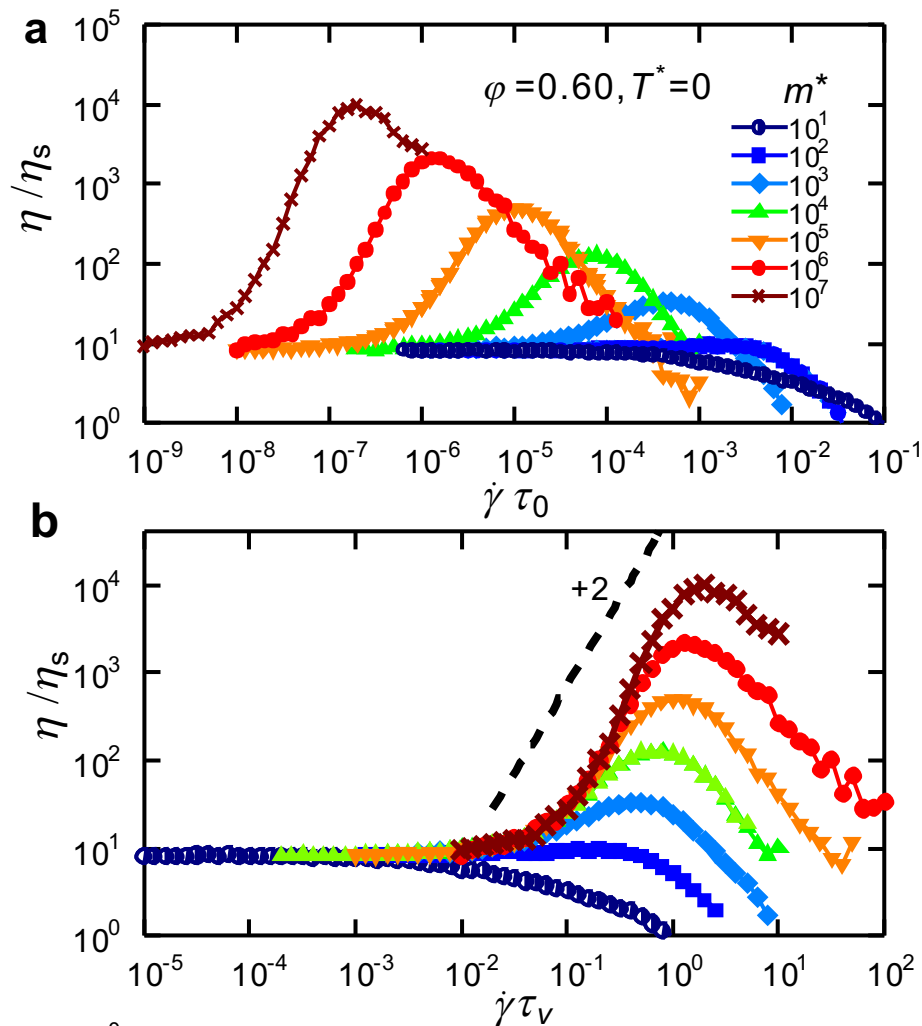


'Jamming phase diagram'



Inertia adds a 3rd timescale

- Rheology for $(T = 0, \varphi = 0.60)$ and increasing m .



- Crossover from Newtonian to **shear-thickening** flow when $\dot{\gamma} \propto 1/\tau_v = \xi/m$ (prefactor ≈ 0.01).

- (i) Energy balance:

$$\sigma \dot{\gamma} \approx \rho L^3 \xi \bar{v}^2 / L^3.$$

- (ii) Momentum exchange via collisions: $\sigma \approx \rho L^2 \bar{v} m \dot{\gamma} a / L^2$

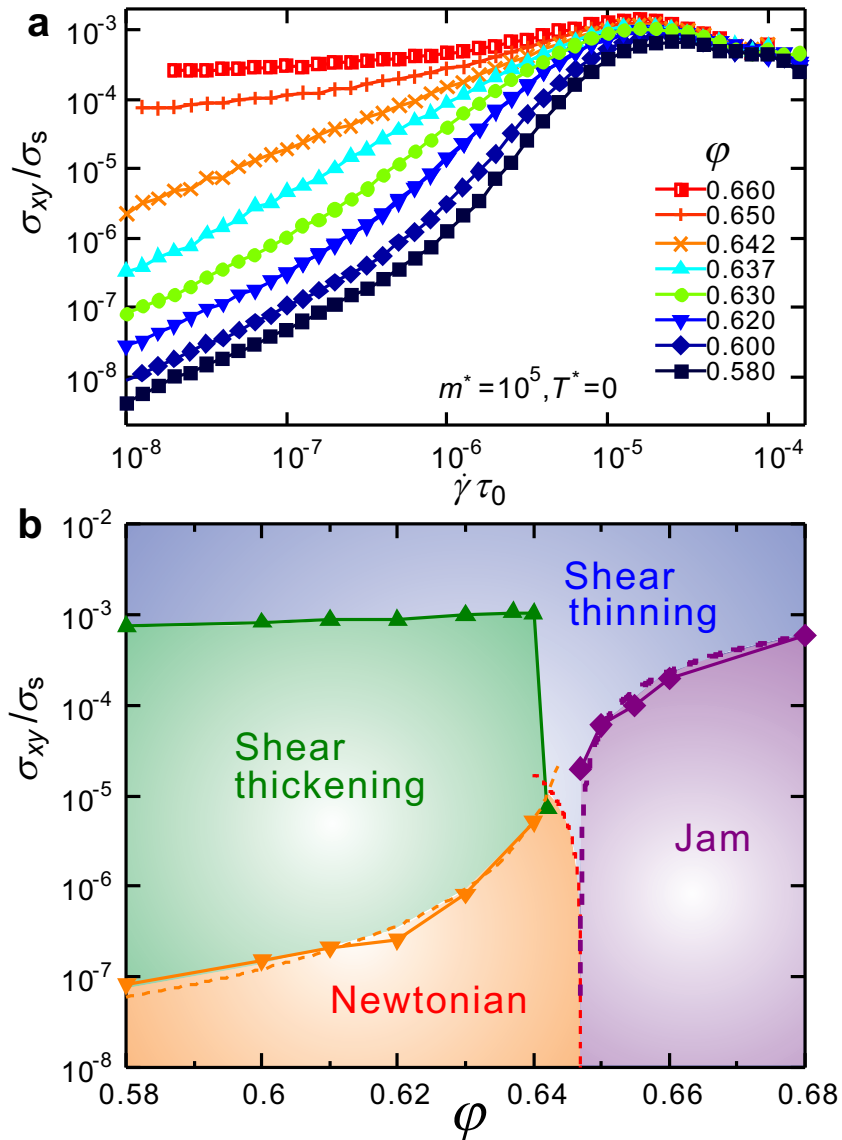
- (i) + (ii) $\rightarrow$ 'Bagnold' scaling:

$$\sigma \approx (\rho m^2 a^2 / \xi) \dot{\gamma}^3, \text{ i.e. } \eta \propto (\dot{\gamma} \tau_v)^2.$$

- Softness controls viscosity maximum: $m \bar{v}^2 / 2 \approx \epsilon$.

[Kawasaki, Ikeda, Berthier, arXiv:1404.4778]

Dynamic 'phase diagram'



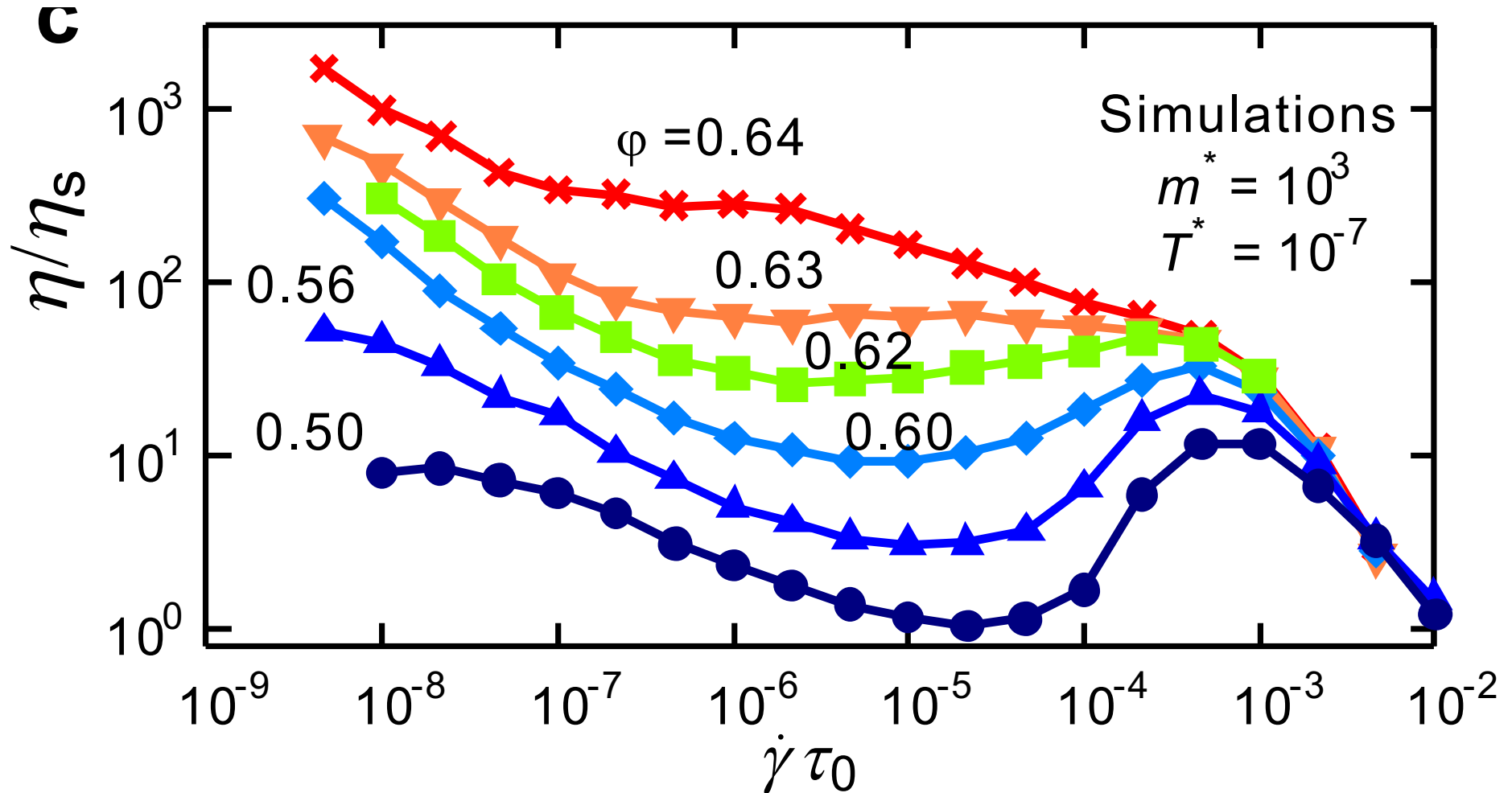
- Shear-thickening observed when $\tau_v^{-1} \ll \dot{\gamma} \ll \dot{\gamma}_c$, and if no additional stress scale.

- Above jamming at $T = 0$, yield stress $\sigma_Y > 0 \rightarrow$ shear-thinning.

- At finite temperature, thermal yield stress develops: $\rightarrow$ shear-thinning.

- Onset of thickening: $\dot{\gamma} \approx 0.01/\tau_v$. Good agreement for some systems (large emulsions, latex), only qualitative agreement for others (macroscopic hard grains).

Jigsaw falling into place



- Thermal glassy regime: $\dot{\gamma} < 10^{-7}$, athermal overdamped: $10^{-7} < \dot{\gamma} < 10^{-5}$, inertial $\dot{\gamma} > 10^{-5}$, softness maximum: $\dot{\gamma} \approx 10^{-3}$, jamming above $\phi = 0.64$. All in a simple model evolving with Langevin dynamics.